10.4-10.5 Angles in a Polygon

Pre-AP Geometry

Name
Period $\qquad$

## EXPLORE/EXPLAIN

## Sum of the interior angles

Triangle Angle-Sum Theorem states that the sum of the interior angles of a triangle is $180^{\circ}$. Now you can use this theorem to investigate the sum of the measures of the interior angles of any polygon.

Work with a partner. Record your data in the table below.
a. Sketch polygons with $4,5,6,7$, and 8 below.
b. Divide each polygon into triangles by drawing all the diagonals from one vertex.
c. Multiply the number of triangles by $180^{\circ}$ to find the sum of the measures of the interior angles of each polygon.
d. Write a conjecture for finding the sum of the measures of the interiors angles of a polygon with " $n$ " sides.

| Name of polygon | Sketch of polygon | Number of sides | Number of <br> triangles formed | Sum of the <br> interior angle <br> measures |
| :---: | :---: | :---: | :--- | :--- |
| Quadrilateral | Pentagon |  | 4 |  |
|  |  |  |  |  |
|  |  |  |  |  |
| n-gon |  |  |  |  |

## Sum of the exterior angles

The figures below show one exterior angle drawn at each vertex of each polygon. Work with your partner and record your data in the table below.
a. Calculate the sum of the measures of the exterior angles of each polygon.
b. Make a conjecture about the sum of the measures of the exterior angles of a polygon with " $n$ " sides.

|  | Column 1 | Column 2 | Exterior Angle Sum |
| :---: | :---: | :---: | :---: |
| Polygons | Sum of the measures of the interior angles | number of linear pairs $\times 180^{\circ}$ | Sum of the exterior angle measures (column 2 column 1) |
| ${ }_{4}^{4}$ | $(m \angle 1+m \angle 2+m \angle 3)=$ $180$ | $3\left(180^{\circ}\right)=540$ | 540-180= |
|  | $(m \angle 1+m \angle 2+m \angle 3+m \angle 4)$ |  |  |
|  |  |  |  |
| n-gon |  |  |  |

